

A Model-Based Approach to Error Budgeting using SysML

Using OMG SysML for performing error accounting for complex systems

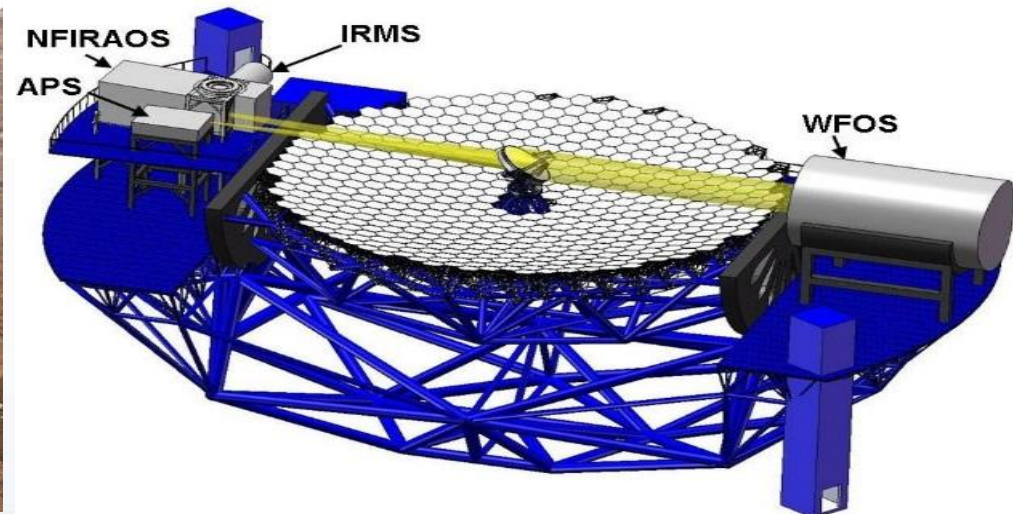
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Outline

- Context
- What is Error Budgeting?
- Motivating Example
- Error Budgeting in SysML
 - ◊ Error Breakdown Tree
 - ◊ Error Roll-Up Pattern
 - ◊ Tying to Requirements & Product Breakdown Structure
- MagicDraw Customizations
- Summary & Conclusions

Context

- ◆ Alignment and Phasing System (APS)
 - ◇ Sensor responsible for measuring the pre-adaptive optics wavefront quality
 - ◇ APS (and AO) team uses MBSE with SysML to analyze requirements, produce design, and perform analysis



Error Budgeting & Error Analysis

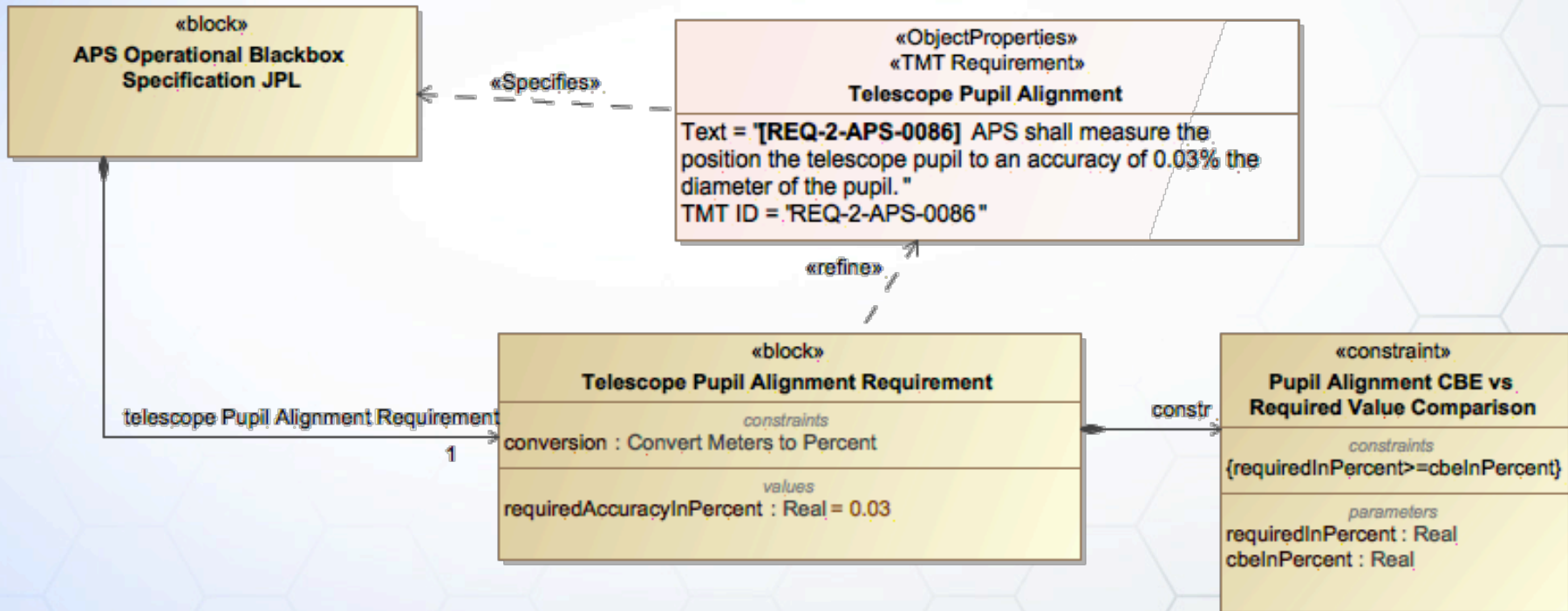
- ◆ Track how accurate expected system performance will be compared to the requirements
- ◆ Error budgeting:
 - ◇ Flow down requirements and allocations
 - ◇ Roll-up capabilities or Current Best Estimates (CBE)
 - ◇ Track margins and reserve
 - ◆ Examples: Mass, Power, Throughput, timing, Pointing Alignment, measurement errors, performance

Challenges

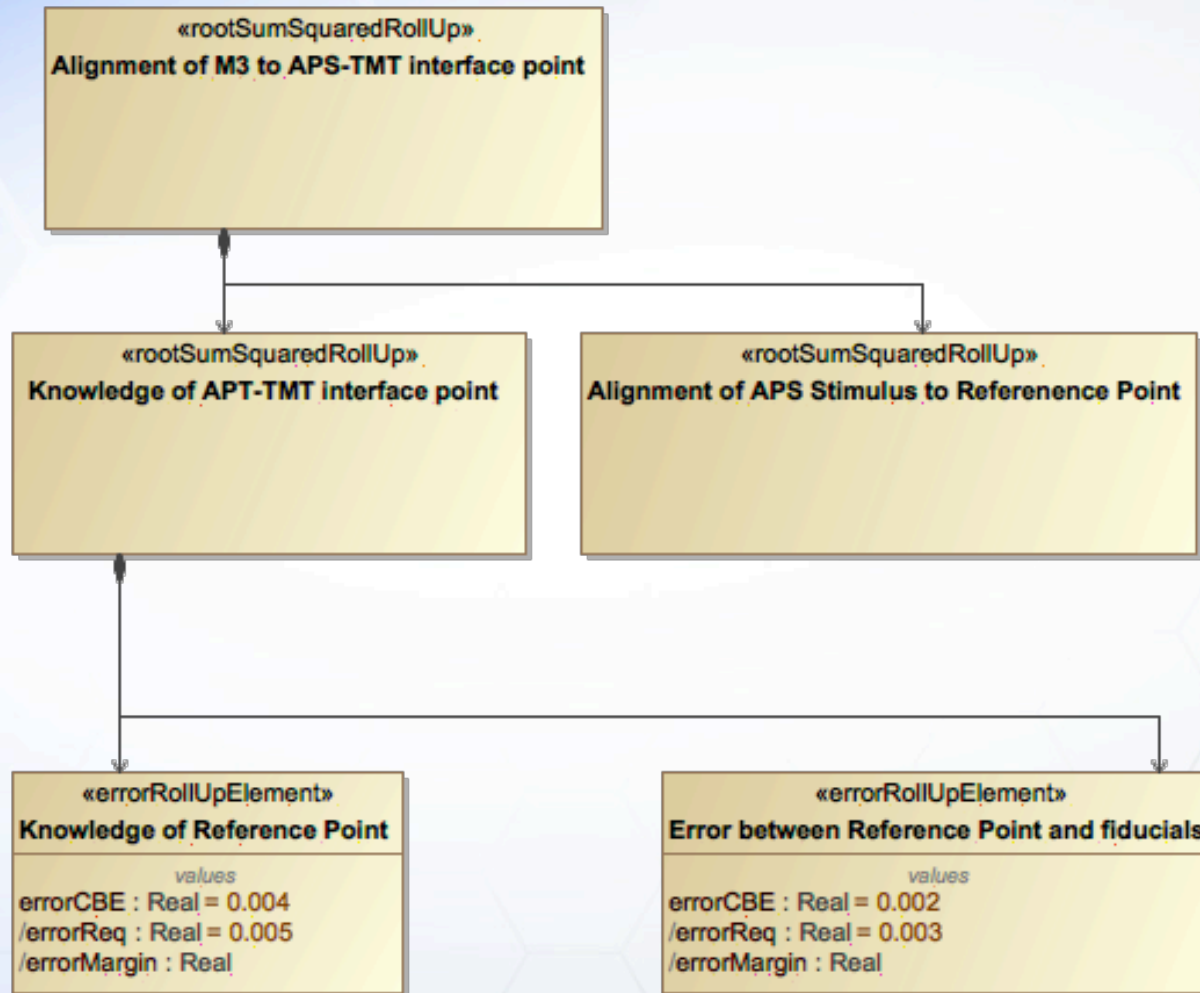
- ◆ Error budget analysis involves multiple, related artifacts:
 - ◇ Requirements ← required accuracy
 - ◇ System design ← current best estimates, parameters
 - ◇ Error decomposition ← roll-up definition
- ◆ CBEs of errors *characterize* errors on properties of the system
- ◆ Decomposition of error != product breakdown structure
 - ➔ Related, but different hierarchies

Motivating Example

- M3 to APS-TMT interface pupil alignment error: *“APS shall measure the position of the telescope pupil to an accuracy of 0.03% of the diameter of the pupil.”*

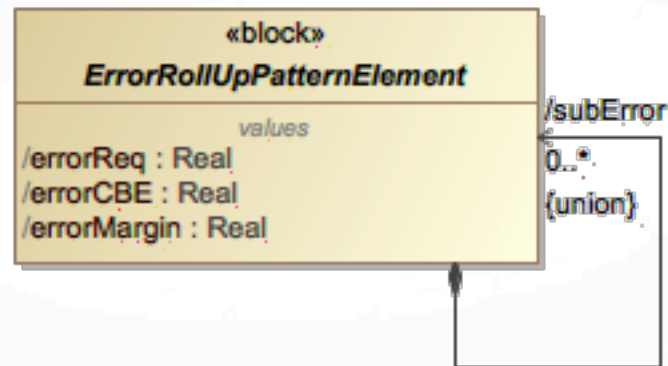


Error Budgeting in SysML: Error Breakdown Tree (Excerpt)



Error Roll-Up Pattern

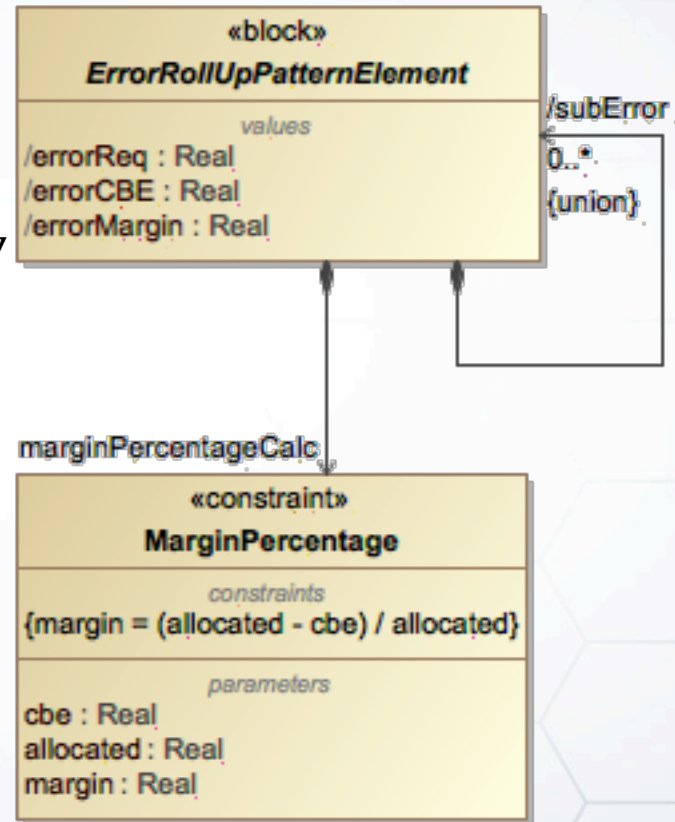
- Similar to mass roll-up pattern



Margin Calculation

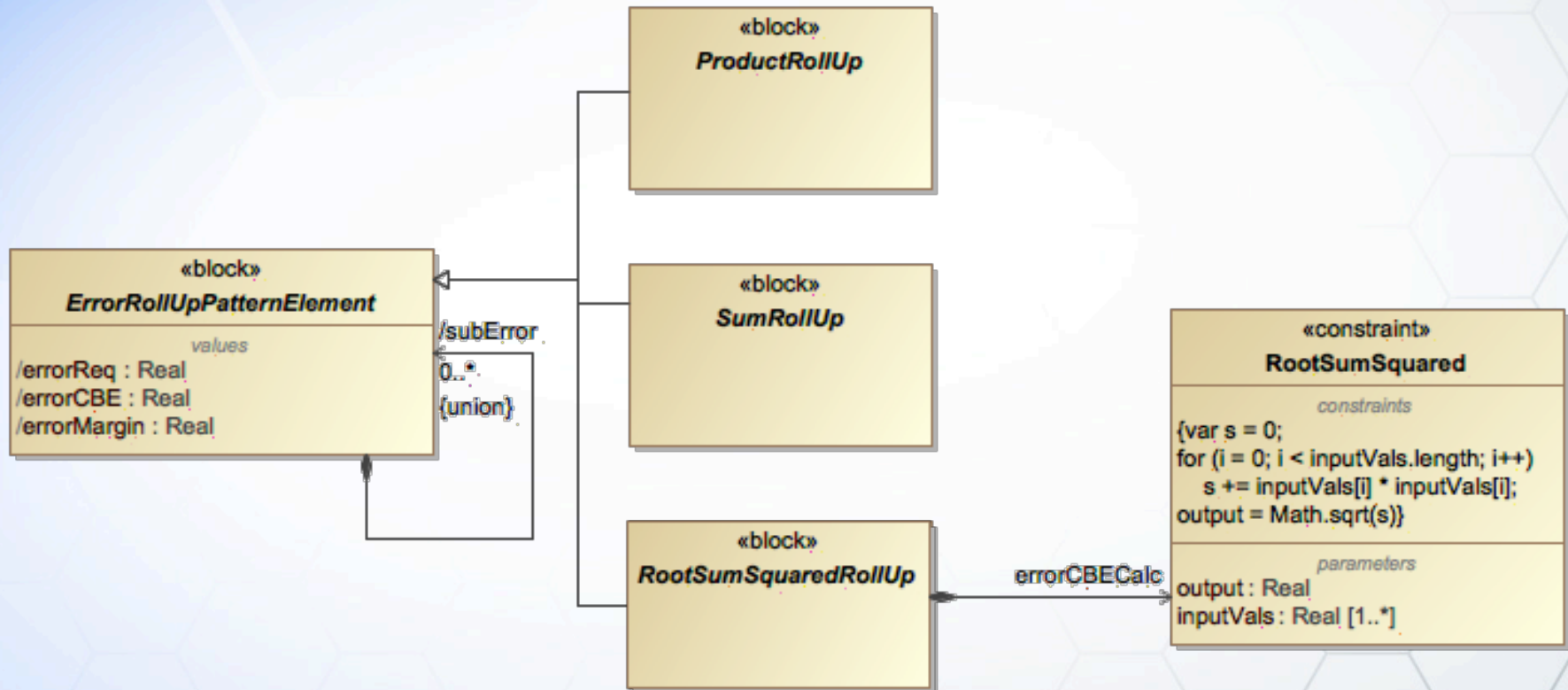
- Margin depends only on CBE and allocation

$$\text{margin} = \text{allocated} - \text{cbe} / \text{allocated}$$



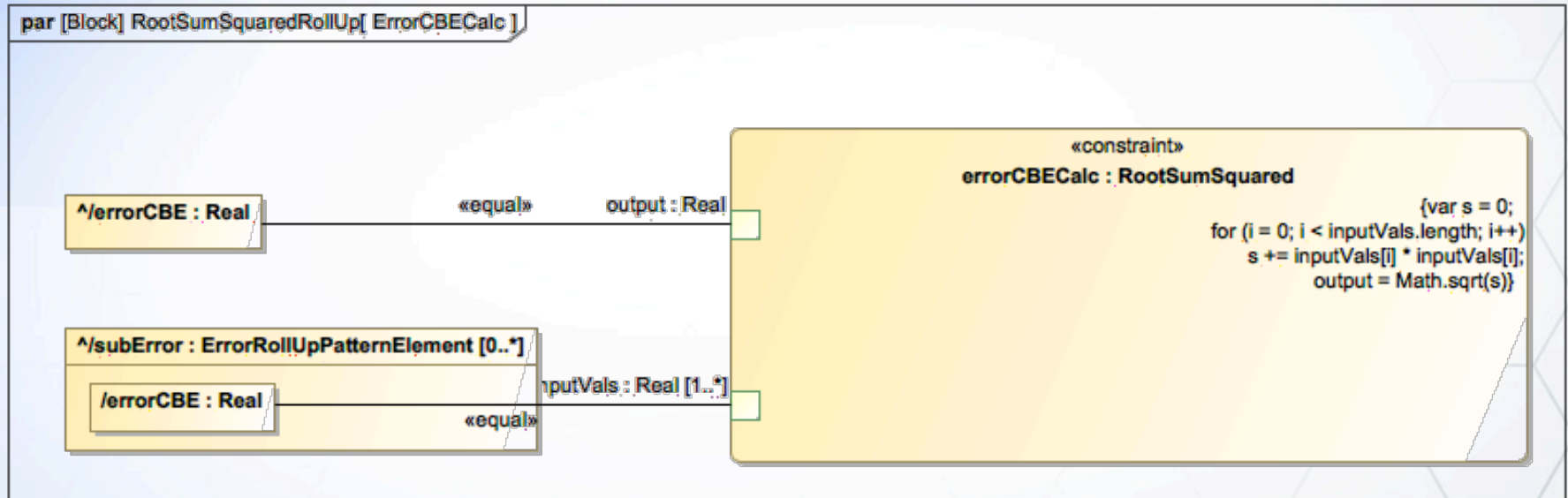
Error Roll-Up Types

- Different roll-up calculations depending on context

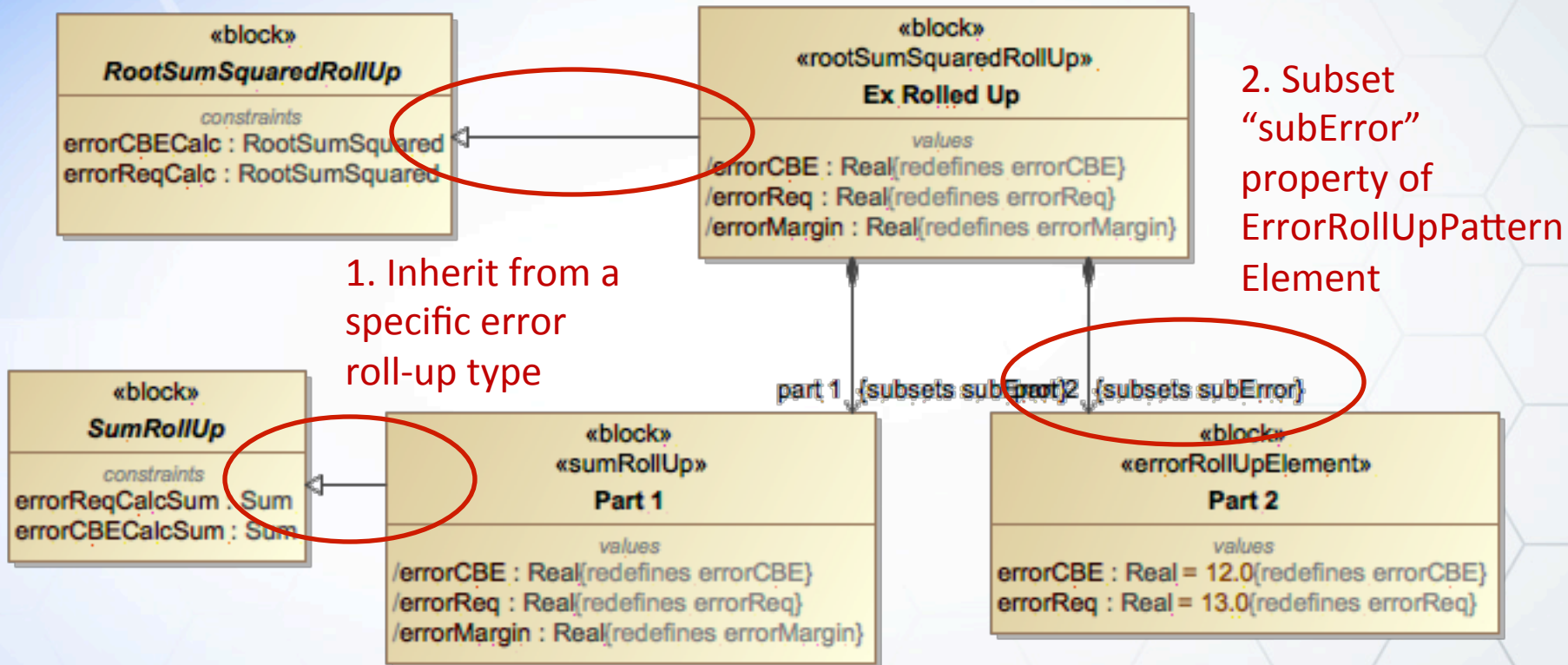


Error Roll-Up Types

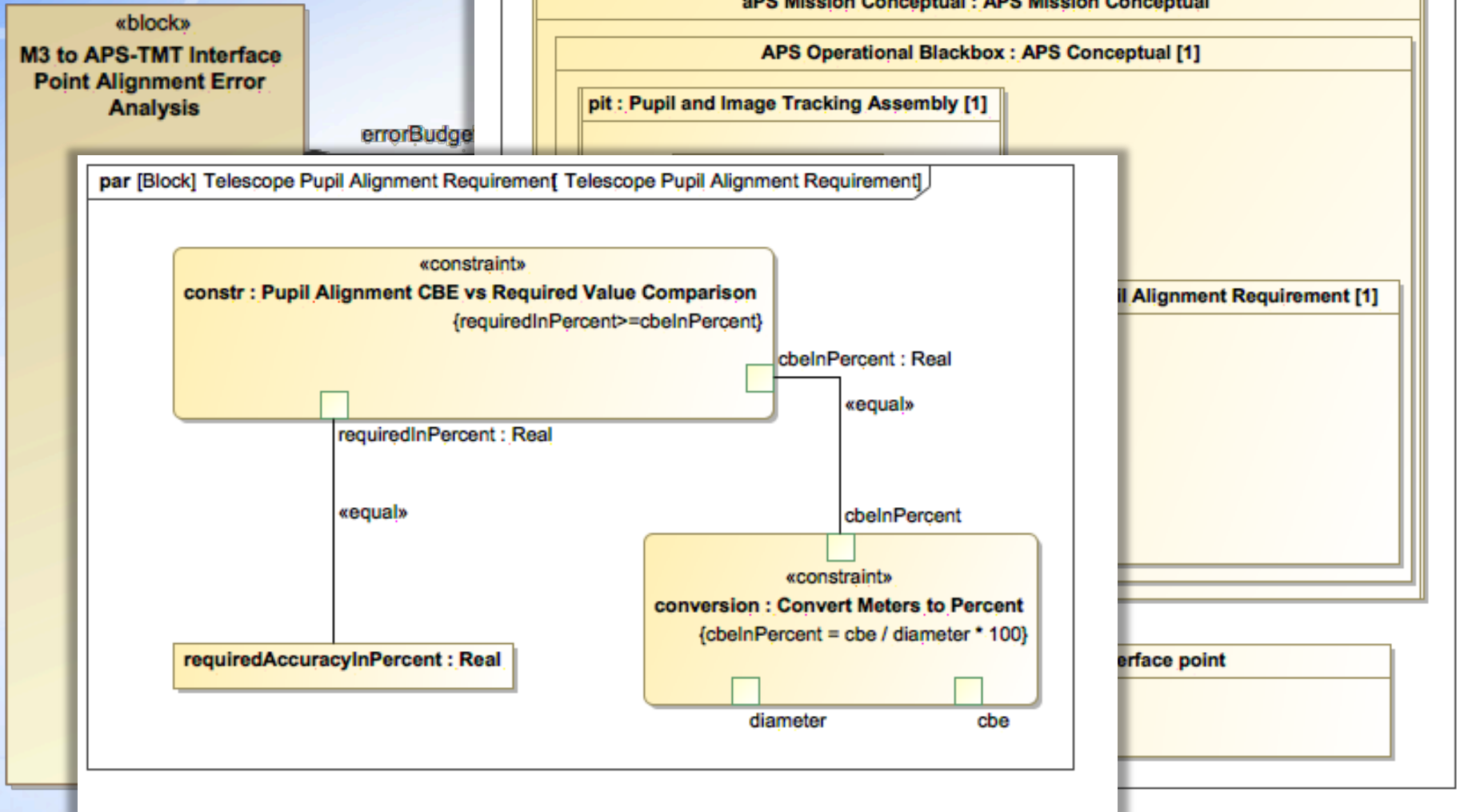
- Different roll-up calculations depending on context



Pattern Application

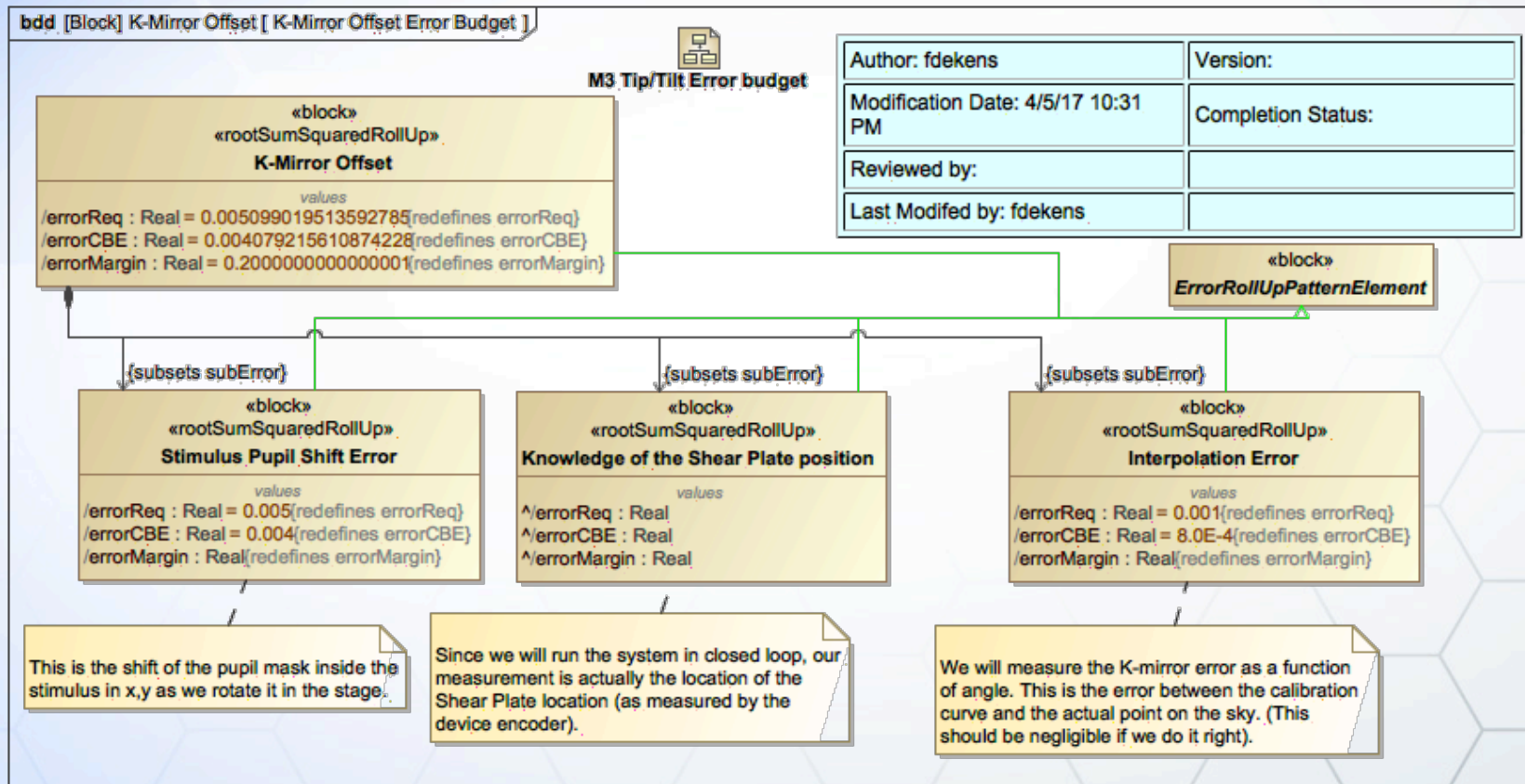


Tying to Requirements & Product Breakdown Structure



Solving & Results

- Parametric solver used for solving set of equations specified in model – here, *Cameo Simulation Toolkit* was used



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1. Formalized requirement

```

«ObjectProperties»
«TMT Requirement»
Telescope Pupil Alignment

Text = [REQ-2-APS-0086] APS shall measure the
position the telescope pupil to an accuracy of 0.03% the
diameter of the pupil.
TMT ID = "REQ-2-APS-0086"
  
```

«refines»

```

«block»
Telescope Pupil Alignment Requirement

constraints
conversion : Convert Meters to Percent

values
requiredAccuracyInPercent : Real = 0.03
  
```

2. Automated roll-up

```

«block»
«rootSumSquaredRollUp»
Alignment of M3 to APS-TMT interface point

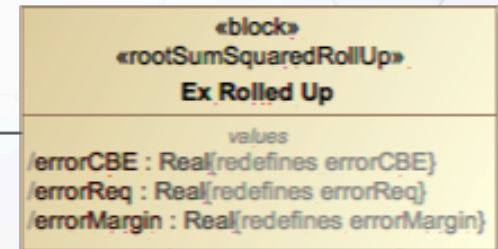
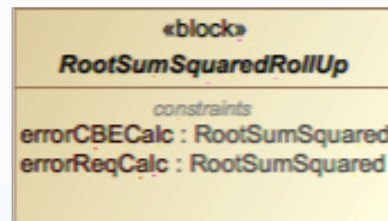
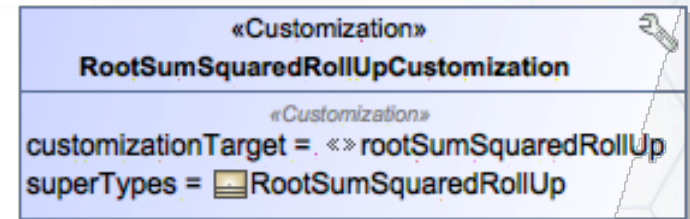
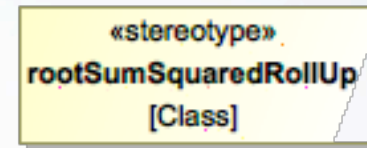
values
/errorMargin : Real = 0.20424201591767288
/errorCBE : Real = 0.012831211945876352
/errorReq : Real = 0.0161245154965971
  
```

3. Automated verification of requirement

#	Name	Constr : Pupil Alignment CBE Vs Required Value Comparison
1	m3 to APS-TMT Interface Point	fail

MagicDraw Customizations

- ◆ If we hide inheritance, how do we know which type of error roll-up was applied?
- ◆ Also, inheritance cumbersome
- ◆ Used stereotypes and MagicDraw DSL customizations to solve both
- ◆ Automatic inheritance from a roll-up type when stereotype is applied
 - ◇ Unfortunately, no solution for subsetting...



How Does the Excel Method Compare to SysML?

● Typical Excel Error Budget

◇ Pros:

- Every one knows Excel!
- Easy to make a copy for what-ifs
- Easy to make changes
- Easy to make yet another error budget (copy one from another project, or from online)
- Extensive math libraries
- Existing tools (queries, linking, etc.)

● Proposed SysML Error Budget

◇ Pros:

- Tied to requirements
- Tied to system design
- Tied to system parameters
- Collaborative
- Version controlled
- Standardized through patterns
- Can be extended to math languages (like Matlab, etc.)

Summary & Conclusions

- ◆ Demonstrated method and pattern for performing error budget analysis within a SysML model
 - ◇ Capture decomposition of error
 - ◇ Perform roll-up of current best estimates of leaf nodes
 - ◇ Calculate margins & verify requirements
- ◆ Method formally ties together requirements on accuracy, system design and relations between errors in an error budget
 - ◇ **Safer** → integration provides less danger of inconsistencies
 - ◇ **Comes at a cost** → careful modeling required

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References

- Open Source TMT model:
<https://github.com/Open-MBEE/TMT-SysML-Model>
- A Practical Guide to SysML, 3rd Edition, Chapter 17 by Friedenthal, Moore, and Steiner

Backup